

## 1. Relaciones entre las razones trigonométricas

$$a) \sin^2 \alpha + \cos^2 \alpha = 1$$

$$b) 1 + \tan^2 \alpha = \sec^2 \alpha$$

$$c) 1 + \cot^2 \alpha = \operatorname{cosec}^2 \alpha$$

$$d) \tan \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$e) \operatorname{cosec} \alpha = \frac{1}{\sin \alpha}$$

$$f) \sec \alpha = \frac{1}{\cos \alpha}$$

$$g) \cot \alpha = \frac{1}{\tan \alpha} = \frac{\cos \alpha}{\sin \alpha}$$

2. Suma de ángulos	3. Ángulo doble	4. Ángulo mitad
$\sin(\alpha + \beta) = \sin \alpha \cdot \cos \beta + \sin \beta \cdot \cos \alpha$	$\sin(2\alpha) = 2 \cdot \sin \alpha \cdot \cos \alpha$	$\sin\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos \alpha}{2}}$
$\cos(\alpha + \beta) = \cos \alpha \cdot \cos \beta - \sin \alpha \cdot \sin \beta$	$\cos(2\alpha) = \cos^2 \alpha - \sin^2 \alpha$	$\cos\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 + \cos \alpha}{2}}$
$\tan(\alpha + \beta) = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \cdot \tan \beta}$	$\tan(2\alpha) = \frac{2 \tan \alpha}{1 - \tan^2 \alpha}$	$\tan\left(\frac{\alpha}{2}\right) = \pm \sqrt{\frac{1 - \cos \alpha}{1 + \cos \alpha}}$

## 5. Transformación de sumas en productos

$$a) \sin A + \sin B = 2 \cdot \sin \frac{A+B}{2} \cdot \cos \frac{A-B}{2}$$

$$b) \sin A - \sin B = 2 \cdot \cos \frac{A+B}{2} \cdot \sin \frac{A-B}{2}$$

$$c) \cos A + \cos B = 2 \cdot \cos \frac{A+B}{2} \cdot \cos \frac{A-B}{2}$$

$$d) \cos A - \cos B = -2 \cdot \sin \frac{A+B}{2} \cdot \sin \frac{A-B}{2}$$

## 6. Signos de las razones trigonométricas

Signos	I Cuad.	II Cuad.	III Cuad.	IV Cuad.
sen	+	+	-	-
cos	+	-	-	+
tan	+	-	+	-
sec	+	-	-	+
cosec	+	+	-	-
cot	+	-	+	-

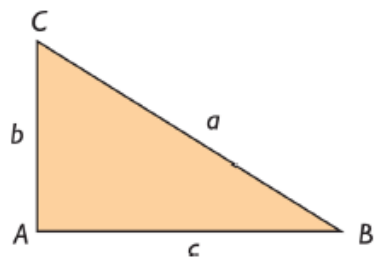
## 7. Relaciones entre los cuatro cuadrantes

sen( $90^\circ - \alpha$ ) = cos $\alpha$ cos( $90^\circ - \alpha$ ) = sen $\alpha$ tan( $90^\circ - \alpha$ ) = cot $\alpha$	sen( $90^\circ + \alpha$ ) = cos $\alpha$ cos( $90^\circ + \alpha$ ) = -sen $\alpha$ tan( $90^\circ + \alpha$ ) = -cot $\alpha$	sen( $180^\circ - \alpha$ ) = sen $\alpha$ cos( $180^\circ - \alpha$ ) = -cos $\alpha$ tan( $180^\circ - \alpha$ ) = -tan $\alpha$	sen( $180^\circ + \alpha$ ) = -sen $\alpha$ cos( $180^\circ + \alpha$ ) = -cos $\alpha$ tan( $180^\circ + \alpha$ ) = +tan $\alpha$
sen( $360^\circ - \alpha$ ) = sen( $-\alpha$ ) = -sen $\alpha$ cos( $360^\circ - \alpha$ ) = cos( $-\alpha$ ) = cos $\alpha$ tan( $360^\circ - \alpha$ ) = tan( $-\alpha$ ) = -tan $\alpha$	sen( $270 - \alpha$ ) = -cos( $\alpha$ ) cos( $270 - \alpha$ ) = -sen( $\alpha$ ) tan( $270 - \alpha$ ) = cot( $\alpha$ )		sen( $270 + \alpha$ ) = -cos( $\alpha$ ) cos( $270 + \alpha$ ) = sen( $\alpha$ ) tan( $270 + \alpha$ ) = -cot( $\alpha$ )

## 8. Razones de los ángulos fundamentales

	$0^\circ$	$30^\circ = \frac{\pi}{6}$	$45^\circ = \frac{\pi}{4}$	$60^\circ = \frac{\pi}{3}$	$90^\circ = \frac{\pi}{2}$	$180^\circ = \pi$	$270^\circ = \frac{3\pi}{2}$	$360^\circ = 2\pi$
sen	0	1/2	$\sqrt{2}/2$	$\sqrt{3}/2$	1	0	-1	0
cos	1	$\sqrt{3}/2$	$\sqrt{2}/2$	1/2	0	-1	0	1
tan	0	$\sqrt{3}/3$	1	$\sqrt{3}$	$\nexists$	0	$\nexists$	0

## 9. Triángulos rectángulos



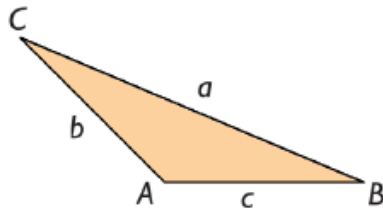
$$\widehat{A} = 90 \quad \text{sen } \widehat{B} = \frac{b}{a}$$

$$\widehat{B} + \widehat{C} = 90 \quad \text{cos } \widehat{B} = \frac{c}{a}$$

$$\widehat{A} + \widehat{B} + \widehat{C} = 180 \quad \text{tan } \widehat{B} = \frac{b}{c}$$

Teorema de Pitágoras:  $a^2 = b^2 + c^2$

## 10. Triángulos oblicuángulos



$$\widehat{A} + \widehat{B} + \widehat{C} = 180$$

Teorema de los senos

$$\frac{a}{\text{sen } \widehat{A}} + \frac{b}{\text{sen } \widehat{B}} + \frac{c}{\text{sen } \widehat{C}}$$

Teorema del coseno

$$a^2 = b^2 + c^2 - 2 \cdot b \cdot c \cdot \text{cos } \widehat{A}$$

$$b^2 = a^2 + c^2 - 2 \cdot a \cdot c \cdot \text{cos } \widehat{B}$$

$$c^2 = a^2 + b^2 - 2 \cdot a \cdot b \cdot \text{cos } \widehat{C}$$